

Complete Solutions Manual for Calculus of a Single Variable, Volume 1

Calculus

ELEVENTH EDITION

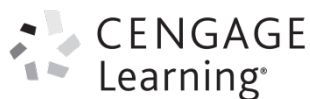
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CHAPTER P

Preparation for Calculus

Section P.1 Graphs and Models

- To find the x -intercepts of the graph of an equation, let y be zero and solve the equation for x . To find the y -intercepts of the graph of an equation, let x be zero and solve the equation for y .
- Substitute the x - and y -values of the ordered pair into both equations. If the ordered pair satisfies both equations, then the ordered pair is a point of intersection.

3. $y = -\frac{3}{2}x + 3$

x -intercept: $(2, 0)$

y -intercept: $(0, 3)$

Matches graph (b).

4. $y = \sqrt{9 - x^2}$

x -intercepts: $(-3, 0), (3, 0)$

y -intercept: $(0, 3)$

Matches graph (d).

5. $y = 3 - x^2$

x -intercepts: $(\sqrt{3}, 0), (-\sqrt{3}, 0)$

y -intercept: $(0, 3)$

Matches graph (a).

6. $y = x^3 - x$

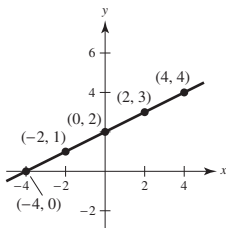
x -intercepts: $(0, 0), (-1, 0), (1, 0)$

y -intercept: $(0, 0)$

Matches graph (c).

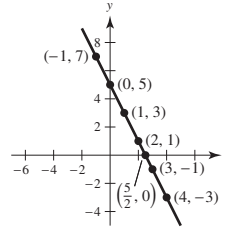
7. $y = \frac{1}{2}x + 2$

x	-4	-2	0	2	4
y	0	1	2	3	4



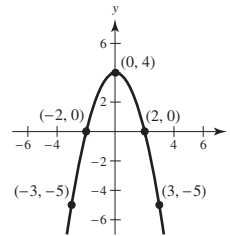
8. $y = 5 - 2x$

x	-1	0	1	2	$\frac{5}{2}$	3	4
y	7	5	3	1	0	-1	-3



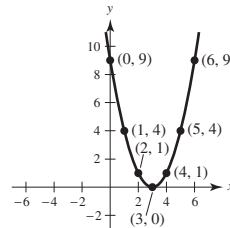
9. $y = 4 - x^2$

x	-3	-2	0	2	3
y	-5	0	4	0	-5



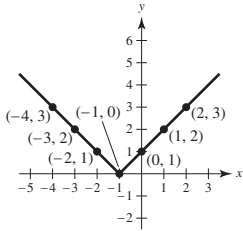
10. $y = (x - 3)^2$

x	0	1	2	3	4	5	6
y	9	4	1	0	1	4	9



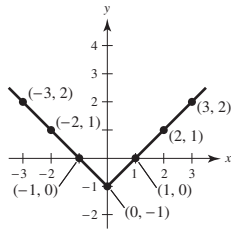
11. $y = |x + 1|$

x	-4	-3	-2	-1	0	1	2
y	3	2	1	0	1	2	3



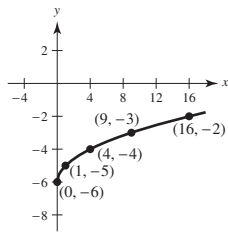
12. $y = |x| - 1$

x	-3	-2	-1	0	1	2	3
y	2	1	0	-1	0	1	2



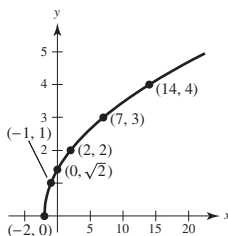
13. $y = \sqrt{x} - 6$

x	0	1	4	9	16
y	-6	-5	-4	-3	-2



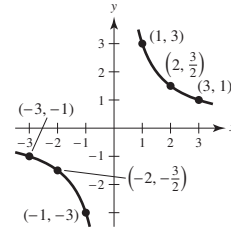
14. $y = \sqrt{x + 2}$

x	-2	-1	0	2	7	14
y	0	1	$\sqrt{2}$	2	3	4



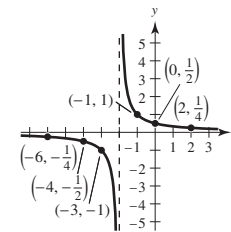
15. $y = \frac{3}{x}$

x	-3	-2	-1	0	1	2	3
y	-1	$-\frac{3}{2}$	-3	Undef.	3	$\frac{3}{2}$	1

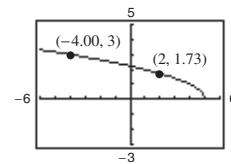


16. $y = \frac{1}{x + 2}$

x	-6	-4	-3	-2	-1	0	2
y	$-\frac{1}{4}$	$-\frac{1}{2}$	-1	Undef.	1	$\frac{1}{2}$	$\frac{1}{4}$



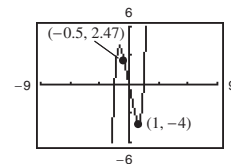
17. $y = \sqrt{5 - x}$



(a) $(2, y) = (2, 1.73)$ ($y = \sqrt{5 - 2} = \sqrt{3} \approx 1.73$)

(b) $(x, 3) = (-4, 3)$ ($3 = \sqrt{5 - (-4)}$)

18. $y = x^5 - 5x$



(a) $(-0.5, y) = (-0.5, 2.47)$

(b) $(x, -4) = (-1.65, -4)$ and $(x, -4) = (1, -4)$

19. $y = 2x - 5$

y-intercept: $y = 2(0) - 5 = -5$; $(0, -5)$

x-intercept: $0 = 2x - 5$

$5 = 2x$

$x = \frac{5}{2}$; $(\frac{5}{2}, 0)$

20. $y = 4x^2 + 3$

y-intercept: $y = 4(0)^2 + 3 = 3$; $(0, 3)$

x-intercept: $0 = 4x^2 + 3$

$-3 = 4x^2$

None. y cannot equal 0.

21. $y = x^2 + x - 2$

y-intercept: $y = 0^2 + 0 - 2$

$y = -2$; $(0, -2)$

x-intercepts: $0 = x^2 + x - 2$

$0 = (x + 2)(x - 1)$

$x = -2, 1$; $(-2, 0), (1, 0)$

22. $y^2 = x^3 - 4x$

y-intercept: $y^2 = 0^3 - 4(0)$

$y = 0$; $(0, 0)$

x-intercepts: $0 = x^3 - 4x$

$0 = x(x - 2)(x + 2)$

$x = 0, \pm 2$; $(0, 0), (\pm 2, 0)$

23. $y = x\sqrt{16 - x^2}$

y-intercept: $y = 0\sqrt{16 - 0^2} = 0$; $(0, 0)$

x-intercepts: $0 = x\sqrt{16 - x^2}$

$0 = x\sqrt{(4 - x)(4 + x)}$

$x = 0, 4, -4$; $(0, 0), (4, 0), (-4, 0)$

24. $y = (x - 1)\sqrt{x^2 + 1}$

y-intercept: $y = (0 - 1)\sqrt{0^2 + 1}$

$y = -1$; $(0, -1)$

x-intercept: $0 = (x - 1)\sqrt{x^2 + 1}$

$x = 1$; $(1, 0)$

25. $y = \frac{2 - \sqrt{x}}{5x + 1}$

y-intercept: $y = \frac{2 - \sqrt{0}}{5(0) + 1} = 2$; $(0, 2)$

x-intercept: $0 = \frac{2 - \sqrt{x}}{5x + 1}$

$0 = 2 - \sqrt{x}$

$x = 4$; $(4, 0)$

26. $y = \frac{x^2 + 3x}{(3x + 1)^2}$

y-intercept: $y = \frac{0^2 + 3(0)}{[3(0) + 1]^2}$

$y = 0$; $(0, 0)$

x-intercepts: $0 = \frac{x^2 + 3x}{(3x + 1)^2}$

$0 = \frac{x(x + 3)}{(3x + 1)^2}$

$x = 0, -3$; $(0, 0), (-3, 0)$

27. $x^2y - x^2 + 4y = 0$

y-intercept: $0^2(y) - 0^2 + 4y = 0$

$y = 0$; $(0, 0)$

x-intercept: $x^2(0) - x^2 + 4(0) = 0$

$x = 0$; $(0, 0)$

28. $y = 2x - \sqrt{x^2 + 1}$

y-intercept: $y = 2(0) - \sqrt{0^2 + 1}$

$y = -1$; $(0, -1)$

x-intercept: $0 = 2x - \sqrt{x^2 + 1}$

$2x = \sqrt{x^2 + 1}$

$4x^2 = x^2 + 1$

$3x^2 = 1$

$x^2 = \frac{1}{3}$

$x = \pm \frac{\sqrt{3}}{3}$

$x = \frac{\sqrt{3}}{3}; \left(\frac{\sqrt{3}}{3}, 0\right)$

Note: $x = -\sqrt{3}/3$ is an extraneous solution.

29. Symmetric with respect to the y -axis because
 $y = (-x)^2 - 6 = x^2 - 6$.

30. $y = 9x - x^2$
 No symmetry with respect to either axis or the origin.

31. Symmetric with respect to the x -axis because
 $(-y)^2 = y^2 = x^3 - 8x$.

32. Symmetric with respect to the origin because
 $(-y) = (-x)^3 + (-x)$
 $-y = -x^3 - x$
 $y = x^3 + x$.

33. Symmetric with respect to the origin because
 $(-x)(-y) = xy = 4$.

34. Symmetric with respect to the x -axis because
 $x(-y)^2 = xy^2 = -10$.

35. $y = 4 - \sqrt{x + 3}$
 No symmetry with respect to either axis or the origin.

36. Symmetric with respect to the origin because
 $(-x)(-y) - \sqrt{4 - (-x)^2} = 0$
 $xy - \sqrt{4 - x^2} = 0$.

37. Symmetric with respect to the origin because
 $-y = \frac{-x}{(-x)^2 + 1}$
 $y = \frac{x}{x^2 + 1}$.

38. Symmetric with respect to the origin because
 $-y = \frac{(-x)^5}{4 - (-x)^2}$
 $-y = \frac{-x^5}{4 - x^2}$
 $y = \frac{x^5}{4 - x^2}$.

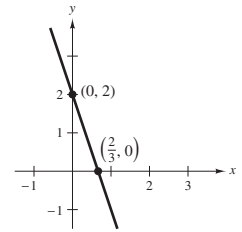
39. $y = |x^3 + x|$ is symmetric with respect to the y -axis
 because $y = |(-x)^3 + (-x)| = |-(x^3 + x)| = |x^3 + x|$.

40. $|y| - x = 3$ is symmetric with respect to the x -axis
 because
 $|-y| - x = 3$
 $|y| - x = 3$.

41. $y = 2 - 3x$
 $y = 2 - 3(0) = 2$, y -intercept
 $0 = 2 - 3(x) \Rightarrow 3x = 2 \Rightarrow x = \frac{2}{3}$, x -intercept

Intercepts: $(0, 2)$, $(\frac{2}{3}, 0)$

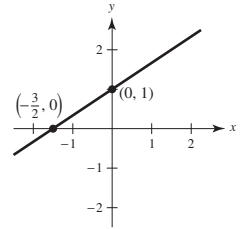
Symmetry: none



42. $y = \frac{2}{3}x + 1$
 $y = \frac{2}{3}(0) + 1 = 1$, y -intercept
 $0 = \frac{2}{3}x + 1 \Rightarrow -\frac{2}{3}x = 1 \Rightarrow x = -\frac{3}{2}$, x -intercept

Intercepts: $(0, 1)$, $(-\frac{3}{2}, 0)$

Symmetry: none

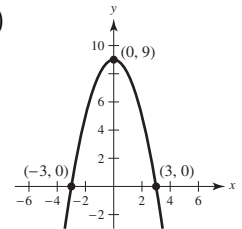


43. $y = 9 - x^2$
 $y = 9 - (0)^2 = 9$, y -intercept
 $0 = 9 - x^2 \Rightarrow x^2 = 9 \Rightarrow x = \pm 3$, x -intercepts

Intercepts: $(0, 9)$, $(3, 0)$, $(-3, 0)$

$y = 9 - (-x)^2 = 9 - x^2$

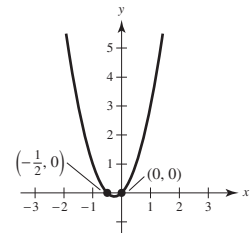
Symmetry: y -axis



44. $y = 2x^2 + x = x(2x + 1)$
 $y = 0(2(0) + 1) = 0$, y -intercept
 $0 = x(2x + 1) \Rightarrow x = 0, -\frac{1}{2}$, x -intercepts

Intercepts: $(0, 0)$, $(-\frac{1}{2}, 0)$

Symmetry: none



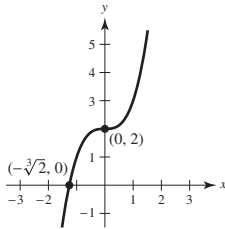
45. $y = x^3 + 2$

$y = 0^3 + 2 = 2$, y -intercept

$0 = x^3 + 2 \Rightarrow x^3 = -2 \Rightarrow x = -\sqrt[3]{2}$, x -intercept

Intercepts: $(-\sqrt[3]{2}, 0)$, $(0, 2)$

Symmetry: none



46. $y = x^3 - 4x$

$y = 0^3 - 4(0) = 0$, y -intercept

$x^3 - 4x = 0$

$x(x^2 - 4) = 0$

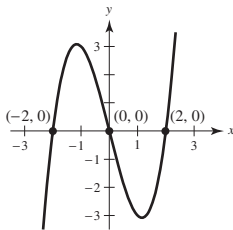
$x(x + 2)(x - 2) = 0$

$x = 0, \pm 2$, x -intercepts

Intercepts: $(0, 0)$, $(2, 0)$, $(-2, 0)$

$y = (-x)^3 - 4(-x) = -x^3 + 4x = -(x^3 - 4x)$

Symmetry: origin



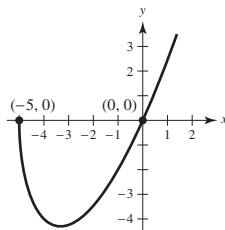
47. $y = x\sqrt{x + 5}$

$y = 0\sqrt{0 + 5} = 0$, y -intercept

$x\sqrt{x + 5} = 0 \Rightarrow x = 0, -5$, x -intercepts

Intercepts: $(0, 0)$, $(-5, 0)$

Symmetry: none



48. $y = \sqrt{25 - x^2}$

$y = \sqrt{25 - 0^2} = \sqrt{25} = 5$, y -intercept

$\sqrt{25 - x^2} = 0$

$25 - x^2 = 0$

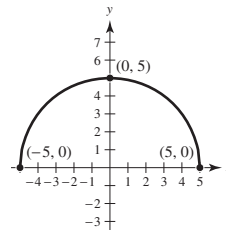
$(5 + x)(5 - x) = 0$

$x = \pm 5$, x -intercept

Intercepts: $(0, 5)$, $(5, 0)$, $(-5, 0)$

$y = \sqrt{25 - (-x)^2} = \sqrt{25 - x^2}$

Symmetry: y -axis



49. $x = y^3$

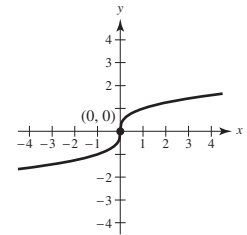
$y^3 = 0 \Rightarrow y = 0$, y -intercept

$x = 0$, x -intercept

Intercept: $(0, 0)$

$-x = (-y)^3 \Rightarrow -x = -y^3$

Symmetry: origin



50. $x = y^4 - 16$

$y^4 - 16 = 0$

$(y^2 - 4)(y^2 + 4) = 0$

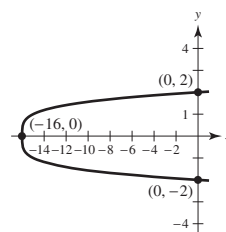
$(y - 2)(y + 2)(y^2 + 4) = 0$

$y = \pm 2$, y -intercepts

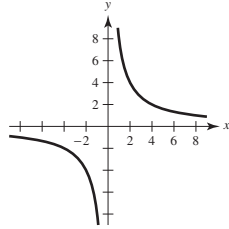
$x = 0^4 - 16 = -16$, x -intercept

Intercepts: $(0, 2)$, $(0, -2)$, $(-16, 0)$

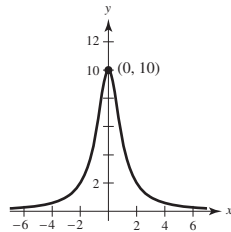
Symmetry: x -axis because $x = (-y)^4 - 16 = y^4 - 16$



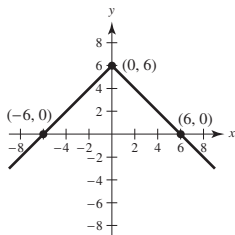
51. $y = \frac{8}{x}$
 $y = \frac{8}{0} \Rightarrow$ Undefined \Rightarrow no y -intercept
 $\frac{8}{x} = 0 \Rightarrow$ No solution \Rightarrow no x -intercept
 Intercepts: none
 $-y = \frac{8}{-x} \Rightarrow y = \frac{8}{x}$
 Symmetry: origin



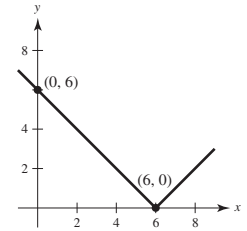
52. $y = \frac{10}{x^2 + 1}$
 $y = \frac{10}{0^2 + 1} = 10$, y -intercept
 $\frac{10}{x^2 + 1} = 0 \Rightarrow$ No solution \Rightarrow no x -intercepts
 Intercept: (0, 10)
 $y = \frac{10}{(-x)^2 + 1} = \frac{10}{x^2 + 1}$
 Symmetry: y -axis



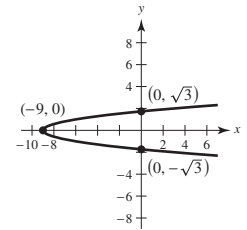
53. $y = 6 - |x|$
 $y = 6 - |0| = 6$, y -intercept
 $6 - |x| = 0$
 $6 = |x|$
 $x = \pm 6$, x -intercepts
 Intercepts: (0, 6), (-6, 0), (6, 0)
 $y = 6 - |-x| = 6 - |x|$
 Symmetry: y -axis



54. $y = |6 - x|$
 $y = |6 - 0| = |6| = 6$, y -intercept
 $|6 - x| = 0$
 $6 - x = 0$
 $6 = x$, x -intercept
 Intercepts: (0, 6), (6, 0)
 Symmetry: none



55. $3y^2 - x = 9$
 $3y^2 = x + 9$
 $y^2 = \frac{1}{3}x + 3$
 $y = \pm\sqrt{\frac{1}{3}x + 3}$
 $y = \pm\sqrt{0 + 3} = \pm\sqrt{3}$, y -intercepts
 $\pm\sqrt{\frac{1}{3}x + 3} = 0$
 $\frac{1}{3}x + 3 = 0$
 $x = -9$, x -intercept
 Intercepts: $(0, \sqrt{3})$, $(0, -\sqrt{3})$, $(-9, 0)$
 $3(-y)^2 - x = 3y^2 - x = 9$
 Symmetry: x -axis



56. $x^2 + 4y^2 = 4 \Rightarrow y = \pm\frac{\sqrt{4 - x^2}}{2}$
 $y = \pm\frac{\sqrt{4 - 0^2}}{2} = \pm\frac{\sqrt{4}}{2} = \pm 1$, y -intercepts
 $x^2 + 4(0)^2 = 4$
 $x^2 = 4$
 $x = \pm 2$, x -intercepts
 Intercepts: (-2, 0), (2, 0), (0, -1), (0, 1)
 $(-x)^2 + 4(-y)^2 = 4 \Rightarrow x^2 + 4y^2 = 4$
 Symmetry: origin and both axes

