# Introduction to Statistics and Data Analysis 6th Edition Roxy Peck <br> California Polytechnic State <br> University, San Luis Obispo 

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ISBN-13: 978-1-337-79417-6
ISBN-10: 1-337-79417-1

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## Chapter 1 The Role of Statistics and the Data Analysis Process

1.1 Descriptive statistics is the branch of statistics that involves the organization and summary of the values in a data set. Inferential statistics is the branch of statistics concerned with reaching conclusions about a population based on the information provided by a sample.
1.2 The population is the entire collection of individuals or objects about which information is required. A sample is a subset of the population selected for study in some prescribed manner.
1.3 The proportions are stated as population values (although they were very likely calculated from sample results).
1.4 The sample is the set of 2121 children used in the study. The population is the set of all children between the ages of one and four.
1.5 a The population of interest is the set of all 15,000 students at the university.
b The sample is the 200 students who are interviewed.
1.6 The estimates given were computed using data from a sample.
1.7 The population is the set of all 7000 property owners. The sample is the 500 owners included in the survey.
1.8 The population is the set of all 2019 Toyota Camrys. The sample is the set of six cars that are tested.
1.9 The population is the set of 5000 used bricks. The sample is the set of 100 bricks she checks.
1.10 a The researchers wanted to know whether the new surgical approach would improve memory functioning in Alzheimer's patients. They hoped that the negative effects of the disease could be reduced by toxins being drained from the fluid filled space that cushions the brain.
b First, it is not stated that the patients were randomly assigned to the treatments (new approach and standard care); this would be necessary in a well designed study. Second, it would help if the experiment could have been designed so that the patients did not know whether they were receiving the new approach or the standard care; otherwise, it is possible that the patients' knowledge that they were receiving a new treatment might in itself have brought about an improvement in memory. Third, as stated in the investigators' conclusion, it would have been useful if the experiment had been conducted on a sufficient number of patients so that any difference observed between the two treatments could not have been attributed to chance.
1.11 a The researchers wanted to find out whether taking a garlic supplement reduces the likelihood that you will get a cold. They wanted to know whether a significantly lower proportion of people who took a garlic supplement would get a cold than those who did not take a garlic supplement.
b It is necessary that the participants were randomly assigned to the treatment groups. If this was the case, it seems that the study was conducted in a reasonable way.
1.12 a Numerical (discrete)
b Categorical
c Numerical (continuous)
d Numerical (continuous)
e Categorical
1.13 a Categorical
b Categorical
c Numerical (discrete)
d Numerical (continuous)
e Categorical
f Numerical (continuous)
1.14 a Discrete
b Continuous
c Discrete
d Discrete
1.15 a Continuous
b Continuous
c Continuous
d Discrete
1.16 For example:
a Ford, Toyota, Ford, General Motors, Chevrolet, Chevrolet, Honda, BMW, Subaru, Nissan.
b $3.23,2.92,4.0,2.8,2.1,3.88,3.33,3.9,2.3,3.56,3.32,2.4,2.8,3.9,3.12$.
c $4,2,0,6,3,3,2,4,5,0,8,2,5,3,4,7,3,2,0,1$
d $50.27,50.67,48.98,50.58,50.95,50.95,50.21,49.70,50.33,49.14,50.83,49.89$
e In minutes: $10,10,18,0,17,17,0,17,12,19,12,13,15,15,15$
1.17 a Gender of purchaser, brand of motorcycle, telephone area code
b Number of previous motorcycles
c Bar chart
d Dotplot
1.18 a


Best Long-Term Investment
b Over half of the responses ( $57 \%$ ) were from people who indicated that the best long-term investments were real estate ( $35 \%$ ) and stocks \& mutual funds ( $22 \%$ ). The remaining $43 \%$ of respondents indicated that gold ( $17 \%$ ), savings ( $15 \%$ ), bonds ( $7 \%$ ), and other ( $4 \%$ ) were the best long-term investments.
1.19 a The dotplot below shows the concussion rate (concussions per 10,000 athletes).

b The dotplot below shows the concussion rate (concussions per 10,000 athletes), with different symbols for boys and girls.


The sport with an unusually high (compared to all the other sports) concussion rate is football. Without considering football, the concussion rates for girls' sports is essentially the same as the concussion rate for boys' sports. However, if we consider football, the concussion rate for girls' sports tends to be lower than that for boys' sports.
1.20 Dotplots (for parts $\mathbf{a}$ and $\mathbf{b}$ ) drawn on the same scale for the 2014 and 2015 sales data are shown below.

a A typical sales figure for 2014 was around 215 million dollars, with sales figures ranging from around 150 to around 350 million dollars. The greatest density of points was at the lower end of the distribution. There were no extreme observations in 2014.
b A typical sales figure for 2015 was around 200 million dollars, with sales figures ranging from around 155 to around 937 million dollars. The greatest density of points was at the lower end of the distribution. There are two extreme observations in 2015, namely, 936.7 million dollars and 652.3 million dollars.
c Sales figures were generally speaking higher in 2015 than in 2014. There were two extreme observations in 2015, and no extreme observations in 2014. If the extreme sales figures are taken into account, the variation in the sales figures (among the top 20 movies) was far greater in 2015 than in 2014. If the extreme sales figures are disregarded, the variation was still greater in 2015 than in 2014, but by not nearly as much. The distributions are similar in shape, with the greatest density of points being at the lower end of the distribution in both cases.
1.21 a

b The most common response was "A lot of thought", accounting for 130 (or 65\%) of the students who started college but did not complete a degree. The next two most common responses were "Some thought" and "No thought", accounting for 48 (or 24\%) and 18 (or $9 \%$ ), respectively, of the students who started college but did not complete a degree. Finally,

4 of the 200 respondents ( $2 \%$ ) indicated that don't know how much thought they have given to going back to school.
1.22 a Categorical
b Since the variable being graphed is categorical, a dotplot would not be suitable.
c If you add up the relative frequencies you get $107 \%$. This total should be $100 \%$, so a mistake has clearly been made.
1.23 a The dotplot shows that there were three sites that received far greater numbers of visits than the remaining 6 sites. Also, it shows that the distribution of the number of visits has the greatest density of points for the smaller numbers of visits, with the density decreasing as the number of visits increases.
b It is clear from the dotplot that there were two sites that were used by far greater numbers of individuals (unique visitors) than the remaining 7 sites. However, these two sites are less far above the others in terms of the number of unique visitors than they are in terms of the total number of visits. As with the distribution of the total number of visits, the distribution of the number of unique visitors has the greatest density of points for the smaller numbers of visitors, with the density decreasing as the number of unique visitors increases. This is the case even when only the 7 less popular sites are considered.
c The statistic "visits per unique visitor" tells us how heavily the individuals are using the sites. The table tells us that the most popular sites (Facebook and YouTube) in terms of total visits and unique visitors do not have the highest value of this statistic. The dotplot of visits per unique visitor shows that there are two individual sites are far ahead of the rest in this respect (Pinterest and Twitter).

### 1.24


1.25 a

b Seventy-five percent (75\%) of the dry weather ratings are B or higher, and $70 \%$ of wet weather ratings are $B$ or higher, indicating that dry weather ratings are higher than wet weather ratings. Note that the wet weather ratings are only $\mathrm{A}+$ or F , so the wet weather ratings are more extreme than dry weather ratings. If we only consider A+ ratings, then the wet weather ratings tend to be better than dry weather ratings because only $55 \%$ of dry weather ratings are A+, compared with $70 \%$ of wet weather ratings being A+.
1.26 a

b Looking at the dotplot we can see that Eastern states have, on average, lower wireless percents than states in the other two regions. The West and Middle states regions have, on average, roughly equal wireless percents.
1.27 a


Three schools seem to stand out from the rest, these being, in increasing order of number of crimes, University of Central Florida ( 14 crimes reported), Florida International University ( 15 crimes reported), and Florida State University ( 20 crimes reported).
b

| University/College | Violent Crime Rate <br> Per 1000 Students |
| :--- | :---: |
| Florida A\&M University | 0.60435 |
| Florida Atlantic University | 0.19750 |
| Florida Gulf Coast University | 0.20225 |
| Florida International University | 0.30131 |
| Florida South Western State College | 0.00000 |
| Florida State University, Tallahassee | 0.48984 |
| New College of Florida | 1.16144 |
| Pensacola State College | 0.00000 |
| Santa Fe College | 0.00000 |
| Tallahassee Community College | 0.16071 |
| University of Central Florida | 0.22239 |
| University of Florida | 0.19745 |
| University of North Florida | 0.19139 |
| University of South Florida, St. Petersburg | 0.00000 |
| University of South Florida, Tampa | 0.19017 |
| University of West Florida | 0.78351 |



The colleges that stand out in violent crimes per 1000 students are, in increasing order of crime rate, Florida State University, Florida A\&M University, University of West Florida, and New College of Florida. Only Florida State University stands out in both dotplots.
c For the number of violent crimes, there are three schools that stand out by having high numbers of crimes, with the majority of the schools having similar, and low ( 10 or fewer), numbers of crimes. There seems to be greater consistency for crime rate (per 1000 students) among the 16 schools than there is for number of crimes, with four schools standing out as having high crime rates, and four schools with crime rates that stand out as being noticeably low.
1.28 a When ranking the airlines according to delayed flights, one airline would be ranked above another if the probability of a randomly chosen flight being delayed is smaller for the first airline than it is for the second airline. These probabilities are estimated using the rate per 10,000 flights values, and so these are the data that should be used for this ranking. (Note that the total number of flights values are not suitable for this ranking. Suppose that one airline had a larger number of delayed flights than another airline. It is possible that this could be accounted for merely through the first airline having more flights than the second.)
b There are two airlines, ExpressJet and Continental, which, with 4.9 and 4.1 of every 10,000 flights delayed, stand out as the worst airlines in this regard. There are two further airlines that stand out above the rest: Delta and Comair, with rates of 2.8 and 2.7 delayed flights per

10,000 flights. All the other airlines have rates below 1.6, with the best rating being for Southwest, with a rate of only 0.1 delayed flights per 10,000 .
1.29 a

b Most public community college graduates have no debt at all, and a debt of $\$ 10,000$ or less accounts for $79 \%$ of the graduates. Among the $21 \%$ of the graduates who have a debt of more than $\$ 10,000$, nearly $43 \%$ ( $9 \%$ of all graduates) have a debt of more than $\$ 20,000$.
1.30 a

b By far the most popular place to buy books is the campus bookstore, with half of the students in the sample buying their books from that source. The next most popular sources are online bookstores other than the online version of the campus bookstore and off-campus bookstores,
with these two sources accounting for around $35 \%$ of students. Purchasing mostly eBooks was the least common response.
1.31 a

| How Often | Relative <br> Frequency |
| :--- | :---: |
| More than once a <br> week | 0.10 |
| Once a week | 0.53 |
| Every other week | 0.26 |
| Every three weeks | 0.05 |
| Less often than every <br> three weeks | 0.06 |

b


How often do you change the sheets?
1.32 The relative frequency distribution is:

| Rating | Relative Frequency |
| :---: | :---: |
| G | $1 / 25=0.04$ |
| PG | $6 / 25=0.24$ |
| PG-13 | $13 / 25=0.52$ |
| R | $5 / 25=0.20$ |



PG-13 is the rating with the highest relative proportion (0.52), followed by PG (0.24), R (0.20), and G (0.04). Seventy-two percent ( $72 \%$ ) of the top 25 movies of 2015 are PG-13 or R, and the remaining $28 \%$ are rated G or PG .
1.33 a The dotplot for Los Angeles County is shown below.


A typical percent of tests failing for Los Angeles County is around 16. There is one value that is unusually high (43), with the other values ranging from 2 to 33 . There is a greater density of points toward the lower end of the distribution than toward the upper end.
b The dotplot for the other counties is shown below.


A typical percent of tests failing for the other counties is around 3. There is one extreme result at the upper end of the distribution (40); the other values range from 0 to 17. The density of points is highest at the left hand end of the distribution and decreases as the percent failing values increase.
c The typical value for Los Angeles County (around 16) is greater than for the other counties (around 3) and, disregarding the one extreme value in each case, there is a greater variability in the values for Los Angeles County than for the other counties. In the distribution for Los Angeles County the points are closer to being uniformly distributed than in the distribution for the other counties, where there is a clear tail-off of density of points as you move to the right of the distribution.

### 1.34 a Categorical

b

c No, since dotplots are used for numerical data.

### 1.35


1.36 a

b By far the most frequently occurring violation categories were security (43\%) and maintenance ( $39 \%$ ). The least frequently occurring violation categories were flight operations ( $6 \%$ ) and hazardous materials (3\%).
1.37 a

b A typical acceptance rate for these top 25 schools is around 30, with the great majority of acceptance rates being between 19 and 39. There are no particularly extreme values. The pattern of the points is roughly symmetrical.

### 1.38



