

Answers to the Review Quizzes

## Page 2

1. List some examples of the scarcity that you face.

Examples of scarcity common to students include not enough income to afford both tuition and a car, not enough learning capacity to study for both an economics exam and a chemistry exam in one night, and not enough time to allow for extensive studying and extensive socializing.
2. Find examples of scarcity in today's headlines.

Scarcity is our inability to satisfy all our wants. An example of scarcity is the headline on cbc.ca on September 14, 2017, which states "Ontario won't offer subsidies to lure Amazon." Amazon is searching for a second North American headquarters. With a subsidy from the Ontario government, Ontario faces scarcity because it has less money to satisfy other wants. Without the subsidy, Amazon may locate elsewhere, depriving Ontario of thousands of jobs and potential billions of dollars in investment.
3. Find an example of the distinction between microeconomics and macroeconomics in today's headlines.

Microeconomics: On September 13, 2017, a headline in The Globe and Mail was "A New Problem: How to sell a $\$ 1,300$ iPhone." This story covers a microeconomic topic because it discusses choices made by Apple to make certain features available on the iPhone. It also discusses choices by individuals to buy an iPhone 7, keep an existing iPhone, or buy a smartphone produced by another firm.
Macroeconomics: On September 2, 2017, a headline in The Globe and Mail was "Hot economy briefly boosts the loonie past 81-cent mark." This story covers a macroeconomic topic because it concerns the effect of the Canadian and world economy on the Canadian dollar.

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1. Describe the broad facts about what, how, and for whom goods and services are produced.

What we produce varies over time. In Canada today, services account for 70 percent of production, manufactured goods for 28 percent, and agriculture for 2 percent. What we produce also varies over countries. Agriculture and manufacturing are small percentages of production in rich countries and large percentages of production in poorer countries.
How goods and services are produced is by businesses determining how the factors of production, land, labour, capital, and entrepreneurship, are combined to make the goods and services we consume. Land includes all natural resources, both renewable natural resources such as wood, and nonrenewable natural resources such as natural gas. The quality of labour depends on human capital. In Canada in 2016, 25.3 percent of the adult population had a
university degree, a further 38.4 percent had some post-secondary education, and 94.8 percent had completed high school.
For whom goods and services are produced depends on the incomes that people earn. People with large incomes can buy a wide range of goods and services. People with small incomes can afford a smaller range of goods and services.

## 2. Use headlines from the recent news to illustrate the potential for conflict between self-interest and the social interest.

One example of an issue that illustrates the potential for conflict between self-interest and the social interest is the proposed Trans Mountain Pipeline. In The Globe and Mail on June 3, 2017, the headline "A pipeline rattles the political landscape; Future of Kinder Morgan project is emblematic of debate over resource development across the country" appears. The potential for conflict exists between the self-interest of the potential workers whose employment is being delayed or possibly eliminated and the social interest of those concerned about the environment.

## Page 10

1. Explain the idea of a tradeoff and think of three tradeoffs that you have made today.

A tradeoff is an exchange—giving up one thing to get something else. What is given up is the opportunity cost of whatever is obtained. Three examples of tradeoffs are: a) When a student sleeps in rather than attending his early morning economics class, the student trades additional sleep for study time. The opportunity cost of the decision is the difference between the $A$ and the $C$ he receives on the exam. b) When a student running late for class parks her car illegally, the student trades saving time for the risk of a ticket. The potential opportunity cost of the decision is the goods and services that cannot be purchased if the student receives an expensive parking ticket. c) A student trades higher income by spending time during the day working at a part-time job for less time spent at leisure time. The opportunity cost of the higher income is the leisure time given up.
2. Explain what economists mean by rational choice and think of three choices that you've made today that are rational.

A rational choice is one that compares the costs and benefits and achieves the greatest benefit over cost for the person making the choice. Three rational choices are: a) The choice to skip breakfast to go to class. In this case the benefit is the higher grade in the class and the cost is the breakfast forgone. b) The choice to stop talking with a friend on the phone and start studying for an impending exam. In this case the benefit is the resulting higher grade in the class and the cost is the conversation forgone. c) The choice to do laundry today rather than watch television. In this case the benefit is clean clothes to wear and the cost is the loss of the entertainment the television show would have provided.
3. Explain why opportunity cost is the best forgone alternative and provide examples of some opportunity costs that you have faced today.

When a decision to undertake one activity is made, often many alternative activities are no longer possible. Often these activities are mutually exclusive so only the highest-valued alternative is actually forgone. For instance, the decision to go to a student's 8:30 AM class eliminates the possibility of sleeping in during the hour and of jogging during the hour. But in this case, it is impossible to both sleep in and to jog during the hour, so the opportunity cost of attending class cannot be both activities. The opportunity cost of attending class is only the activity that otherwise would have been chosen-either sleeping in or jogging-whatever activity is the most highly valued of the forgone alternatives.
4. Explain what it means to choose at the margin and illustrate with three choices at the margin that you have made today.
Choosing at the margin means choosing to do a little more or a little less of some activity. Three examples are: a) When a student faces a chemistry and an economics final exam in one day, the student must determine whether spending the last hour studying a little more chemistry or a little more economics will yield a better contribution (marginal benefit) to his overall GPA. b) A student buying a computer must decide whether the marginal benefit from adding 1 GB of additional memory is worth the marginal cost of the additional memory. c) A student football fan with a choice of a cheap seat in the student bleachers located at the far end of the playing field or a more expensive seat located on the 30 yard line must determine whether the marginal benefit from watching the game in a better seat is worth the marginal cost of the higher ticket price.
5. Explain why choices respond to incentives and think of three incentives to which you have responded today.
People making rational decisions compare the marginal benefit from an action to its marginal cost. A person's choice changes when the incentive-the marginal benefit or the marginal cost changes. Examples of incentives are: a) A student studies because of the incentives offered by grades. b) A student is more likely to attend a class if attendance is factored into the grade. c) A student might attend a meeting of a club if the student's significant other is eager to attend the meeting.

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1. Distinguish between a positive statement and a normative statement and provide examples.
A positive statement is about what is. It is testable. A normative statement is about what ought to $b e$. It is not testable because there is no universally approved criterion by which the statement can be judged. "I will receive an A for this course," is a positive statement made by an economics student-it might not be true, but it is testable. "I will receive a good grade for this course," is a normative statement. Whether someone agrees with it depends on his interpretation of what makes for a "good" grade.
2. What is a model? Can you think of a model that you might use in your everyday life?
A model is a description of some aspect of the world. An economic model is a description of some aspect of the economic world that includes only those features that are needed for the purpose at hand. An example of a model is a GPS map. It reflects only those aspects of the real world that are relevant to the user in reaching her destination and avoids information irrelevant to travel.
3. How do economists try to disentangle cause and effect?

Economists disentangle cause and effect by using natural experiments (situations in the ordinary course of economic life in which the one factor of interest is different and other things are equal or similar); conducting statistical investigations to find correlations; and performing economic experiments by putting people in decision-making situations and varying the influence of one factor at a time to discover how they respond.
4. How is economics used as a policy tool?

Individuals, businesses, and governments use economics as a policy tool. Individuals use the economic ideas of marginal benefit and marginal cost when making decisions for such topics as attending university, paying cash or credit for a purchase, and working. Businesses also use the concepts of marginal benefit and marginal cost when making decisions about what to produce, how to produce, and how many hours to stay open. Governments use marginal benefit and marginal cost when deciding issues such as the level of property taxes, the amount to fund higher education, or the level of a tariff on EU imports.

## Page 13

1. What types of jobs do economists do?

Economists do jobs that require the collection and analysis of data on the production and use of resources. They work at jobs that require the ability to predict future trends. Economists are also in jobs that study to determine ways of using resources more efficiently.
Three common jobs that hire economists are market research analyst, financial analyst, and budget analyst.
A market research analyst works with data on buying patterns to forecast the likely success of a product and the price consumers are willing to pay for it.
A financial analyst studies trends and fluctuations in interest rates and stock and bond prices and tries to predict the cost of borrowing and the returns on investments.
A budget analyst keeps track of an organization's cash flow and prepares budget plans that incorporate predictions of future cash flows.
2. What is the range and median level of economists' pay?

The Web resource payscale.com reports a pay range for economists of all types from \$44,441 to $\$ 127,500$, with a median of $\$ 85,970$.
3. What are the skills needed for an economics job?

The five most important skill requirements for an economics job are critical-thinking skills, analytical skills, math skills, writing skills, and oral communication skills.
Critical-thinking skills are the ability to clarify and solve problems using logic and relevant evidence.
Analytical skills are the use of economic ideas and tools to examine data, notice patterns, and reach a logical conclusion.
Math skills are the ability to use mathematical and statistical tools to analyze data and reach valid conclusions.
Writing skills are the ability to present ideas, conclusions, and reasons in succinct written reports appropriate for the target audience.
Oral communication skills are the ability to explain ideas, conclusions, and reasons to people with a limited background in economics.

## Answers to the Study Plan Problems and Applications

1. Apple Inc. decides to make iTunes freely available in unlimited quantities.
a. Does Apple's decision change the incentives that people face?

Apple's decision changes people's incentives. For example, it increases the incentive to buy an iPhone to take advantage of the newly "free" music available on iTunes.
b. Is Apple's decision an example of a microeconomic or a macroeconomic issue? Apple's decision is a microeconomic issue because it affects a single company and a single market.
2. Which of the following pairs does not match?
a. Labour and wages Labour earns wages, so this pair matches.
b. Land and rent Land earns rent, so this pair matches.
c. Entrepreneurship and profit Entrepreneurship earns profit, so this pair matches.
d. Capital and profit Capital earns interest, so this pair does not match.
3. Explain how the following news headlines concern self-interest and the social interest.
a. Starbucks Expands in China Starbucks' expansion is a decision made by Starbucks to further Starbucks' interest. The decision is directly in Starbucks' self-interest. The social interest is affected because Starbucks' expansion will have an effect in China. For example, more Chinese might drink coffee rather than tea and fewer Chinese entrepreneurs will open new coffee shops.
b. McDonald's Moves into Online Ordering

McDonald's decision to move into online ordering is a decision made by McDonald's to further McDonald's interest. The decision is directly in McDonald's self-interest. The social interest could be affected because people will spend less time waiting in lines and drive-throughs.
c. Food Must Be Labelled with Nutrition Data

The decision to require that food must be labelled with nutrition information is made in the social interest. This decision is not made by any one single firm and so does not (necessarily) reflect anyone's self-interest.
4. The night before an economics test, you decide to go to the movies instead of staying home and working your MyLab Study Plan. Your grade on the test was 50 percent, lower than your usual 70 percent score.
a. Did you face a tradeoff?

Yes, you faced a tradeoff. The tradeoff was between a higher test score and an evening with your friends at the movies.
b. What was the opportunity cost of your evening at the movies?

The opportunity cost of going to the movies is the fall in your grade. That is the 20 points forgone from choosing to see the movie rather than study.

## 5. Cost of Rio Olympics

Brazilian federal, state, and local governments spent $\mathrm{R} \$ 2.8$ billion and private sponsors spent $\mathrm{R} \$ 4.2$ billion on 17 new Olympic facilities, 10 of which will be used for sporting events after the Olympics.

Source: Financial Times, August 6, 2016
Was the opportunity cost of the Rio Olympics? Explain your answer.
The opportunity cost of something is the highest-valued alternative that we give up to get it. To host the Olympics in Rio, R\$2.8 was spent by federal, state, and local governments and R\$4.2 billion was spent by local sponsors, a total expenditure of R $\$ 7.0$ billion. The opportunity cost of the Rio Olympics is not the expenditure but the goods and services that would have been purchased with R $\$ 7.0$ billion if the money had not been spent on the Rio Olympics.
6. Which of the following statements is positive, which is normative, and which can be tested?
a. Canada should cut its imports.

The statement is normative and cannot be tested.
b. China is Canada's largest trading partner.

The statement is positive and can be tested.
c. If the price of gasoline rises, people will drive less and use less gasoline.

The statement is positive and can be tested.

## Answers to Additional Problems and Applications

## 7. Kanye West Offers Free Concert Tickets

Kanye West has teamed with Los Angeles inner-city schools to offer free passes for students!

Source: consequenceofsound.net, November 27, 2016

## When Kanye West gave away tickets, what was free and what was scarce? Explain your answer.

The seats in the concert venue are scarce-there are only a limited number available. Also scarce is the time the enthusiastic students spend at the concert. If the students who obtain passes attend the concert rather than sell their "free" passes, they incur the opportunity cost of the forgone pass price. So the concert was not "free" for the concert-goers. The publicity that Kanye West receives is free to him but the publicity used reporters' scarce time to report on the event rather than reporting on other news worthy events.
8. How does the creation of a successful movie influence what, how, and for whom goods and services are produced?

The "what" question is influenced in two ways. First, one good or service that is produced is the successful movie. Second, spinoffs or similar films likely will be created in the future. The "how" question is influenced because movies use different production methods. Some movies, for example, have a lot of special effects while other movies have few or none. The "for whom" question is influenced because those people who, as the result of the blockbuster movie, have higher incomes have more goods and services produced for them.
9. How does a successful movie illustrate self-interested choices that are also in the social interest?

A successful movie increases the income of the people involved with the movie production. The choices of these people are driven largely by self-interest. The creation of a successful movie also increases the quantity of widely enjoyed entertainment. The amount of entertainment available in the economy increases, which benefits society. So the choices the people made in their self-interest are also in the social interest.
10. Before starring in Guardians of the Galaxy, Chris Pratt had appeared in $\mathbf{1 1}$ movies that grossed an average of $\$ 7$ million on the opening weekend. Guardians of the Galaxy grossed $\$ 94$ million.
a. How will the success of Guardians of the Galaxy influence the opportunity cost of hiring Chris Pratt?

The opportunity cost of something is the highest-valued alternative that must be given up to get it.
Based on the success of Guardians of the Galaxy, Chris Pratt will now require a higher salary to star in a movie. The extra money that is paid to Chris Pratt could have been used to hire other actors or to film more on location. The best alternative that is forgone because Chris Pratt is paid more money is the opportunity cost of hiring him.
b. How have the incentives for a movie producer to hire Chris Pratt changed? Because Chris Pratt is now a proven actor who can draw in large first-weekend box office revenues, movie producers have a greater incentive to hire him. Since Guardians of the Galaxy was a hit, it is probable that Chris Pratt's future films will also be hits.
11. What might be an incentive for you to take a class in summer school? List some of the benefits and costs involved in your decision. Would your choice be rational?

Early graduation, smaller class sizes, and retaining eligibility for a scholarship are examples of incentives that encourage taking summer classes. The benefits from taking summer classes might include more personal attention from the instructor and increased knowledge about some aspect of the world. Costs include forgone summer jobs or internships, less time to spend with friends, and additional tuition and other class-related expenses. The choice is rational if the student achieves the greatest benefit over cost.
12. Look at today's National Post. What is the leading economic news story? With which of the big economic questions does it deal and what tradeoffs does it discuss or imply?

On December 5, 2016, a top economic news story discussed was "Amazon testing retail store that eliminates checkout line, charges shoppers as they leave". This news stories answers the following questions:
What goods and services are produced? The news story deals with the production of checkout services by Amazon.
How are goods and services produced? The news story tells that Amazon is producing checkout services using a combination of artificial intelligence software-including computer vision algorithms that enable machines to identify images-and sensors. A tradeoff is giving up one thing to get something else. When Amazon uses cashier-less technology, it gives up using traditional check-out methods.
13. Provide two microeconomic statements and two macroeconomic statements. Classify your statements as positive or normative. Explain why.

Microeconomic statements are: Fewer deep water oil wells should be drilled off the B.C. coast. If less oil is produced, the price of oil will rise. The first statement is normative because it relies on what the person thinks "should" be done. The second statement is positive because it is possible to test the effect of less oil being produced.
Macroeconomic statements are: The current unemployment rate is too high. The current unemployment rate is higher for men than for women. The first statement is normative because it depends on what is deemed "too high." The second statement is positive because it can be checked to determine its validity.

Answers to the Appendix Review Quiz
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1. Explain how we "read" the graphs in Figs. A1.1 and A1.2.

The points in the graphs relate the quantity of the variable measured on the one axis to the quantity of the variable measured on the other axis. The quantity of the variable measured on the horizontal axis (the $x$-axis) is measured by the horizontal distance from the origin to the point. The quantity of the variable measured on the vertical axis (the $y$-axis) is measured by the vertical distance from the origin to the point. The point relates these two quantities. For example, in Figure A1.2a, point $A$ shows that at a price of $\$ 8.43$ a ticket, 1.3 billion movie tickets are sold.
2. Explain what scatter diagrams show and why we use them.

A scatter diagram is a graph that plots the value of one variable against the value of another variable for a number of different values of each variable. We use scatter diagrams because they quickly reveal if a relationship exists between the two variables.
3. Explain how we "read" the three scatter diagrams in Figs. A1.3 and A1.4.

The scatter diagram in Figure A1.3 shows the relationship between production budgets and worldwide box office revenues for ten popular movies. The figure shows no tendency for a larger production budget to bring a greater box office revenue.
The scatter diagram in Figure A1.4a shows the relationship between income measured in thousands of dollars per year, and expenditure measured in thousands of dollars per year, for the years 2005 to 2015. The scatter diagram shows that higher income leads to higher expenditure. The figure also shows this is a close relationship.
The scatter diagram in Figure A1.4b shows the relationship between the unemployment rate and the inflation rate for the years 2006 to 2016. The figure shows that for most of the years, the relationship between inflation and unemployment is weak.
4. Draw a graph to show the relationship between two variables that move in the same direction.

A graph that shows the relationship between two variables that move in the same direction is shown by a line that slopes upward.
5. Draw a graph to show the relationship between two variables that move in opposite directions.

A graph that shows the relationship between two variables that move in opposite directions is shown by a line that slopes downward.
6. Draw a graph of two variables whose relationship shows (i) a maximum and (ii) a minimum.

A graph that shows the relationship between two variables that have a maximum is shown by a curve that starts out sloping upward, reaches a maximum, and then slopes downward.
A graph that shows the relationship between two variables that have a minimum is shown by a curve that starts out sloping downward, reaches a minimum, and then slopes upward.

## 7. Which of the relationships in Questions 4 and 5 is a positive relationship and which is a negative relationship?

The relationship in Question 4 between the two variables that move in the same direction is a positive relationship. The relationship in Question 5 between the two variables that move in opposite directions is a negative relationship.
8. What are the two ways of calculating the slope of a curved line?

To calculate the slope of a curved line we can calculate the slope at a point or across an arc. The slope of a curved line at a point on the line is defined as the slope of the straight line tangent to the curved line at that point. The slope of a curved line across an arc-between two points on the curved line-equals the slope of the straight line between the two points.
9. How do we graph a relationship among more than two variables?

To graph a relationship among more than two variables, hold constant the values of all the variables except two. Then plot the value of one of the variables against the other variable.
10. Explain what change will bring a movement along a curve.

A movement along a curve occurs when the value of a variable measured on one of the axes changes while all of the other relevant variables not graphed on the axes do not change.
11. Explain what change will bring a shift of a curve.

A curve shifts when there is a change in the value of a relevant variable that is not graphed on the axes.

## Answers to the Appendix Study Plan Problems and Applications

Use the spreadsheet to work Problems 1 to 3 . The spreadsheet provides the economic data: Column $A$ is the year, column B is the inflation rate, column $C$ is the interest rate, column D is the growth rate, and column E is the unemployment rate.

1. Draw a scatter diagram of the inflation rate and the interest rate. Describe the

|  | A | B | C | D | E |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2006 | 2.5 | 4.9 | 2.7 | 4.6 |
| 2 | 2007 | 4.1 | 4.5 | 1.8 | 4.6 |
| 3 | 2008 | 0.1 | 1.4 | -0.3 | 5.8 |
| 4 | 2009 | 2.7 | 0.2 | -2.8 | 9.3 |
| 5 | 2010 | 1.5 | 0.1 | 2.5 | 9.6 |
| 6 | 2011 | 3.0 | 0.1 | 1.6 | 8.9 |
| 7 | 2012 | 1.7 | 0.1 | 2.2 | 8.1 |
| 8 | 2013 | 1.5 | 0.1 | 1.7 | 7.4 |
| 9 | 2014 | 0.8 | 0.0 | 2.4 | 6.2 |
| 10 | 2015 | 0.7 | 0.1 | 2.6 | 5.3 |
| 11 | 2016 | 2.1 | 0.3 | 1.6 | 4.9 | relationship.

To make a scatter diagram of the inflation rate and the interest rate, plot the inflation rate on the $x$-axis and the interest rate on the $y$-axis. The graph will be a set of dots. The pattern made by the dots shows a weak positive relationship.
2. Draw a scatter diagram of the growth rate and the unemployment rate. Describe the relationship.

To make a scatter diagram of the growth rate and the unemployment rate, plot the growth rate on the $x$-axis and the unemployment rate on the $y$-axis. The graph will be a set of dots. The pattern made by the dots shows that when the growth rate increases, the unemployment rate usually decreases so there is a negative relationship.
3. Draw a scatter diagram of the interest rate and the unemployment rate. Describe the relationship.

To make a scatter diagram of the interest rate and the unemployment rate, plot the interest rate on the $x$-axis and the unemployment rate on the $y$-axis. The graph will be a set of dots. The pattern made by the dots tells us that when the interest rate increases, the unemployment rate usually decreases so there is a negative relationship.

Use the following news clip to work Problems 4 to 6.

## Kong Tops the Box Office

| Movie | Theatres <br> (number) | Revenue <br> (dollars per <br> theatre) |
| :--- | :---: | :---: |
| Kong: Skull Island | 3,846 | $\$ 15,867$ |
| Logan | 4,071 | $\$ 9,362$ |
| Get Out | 3,143 | $\$ 6,600$ |
| The Shack | 2,888 | $\$ 3,465$ |

Source: boxofficemojo.com
Data for weekend of February 10-12, 2017
4. Draw a graph of the relationship between the revenue per theatre on the $y$-axis and the number of theatres on the $x$-axis. Describe the relationship.

The graph shows a positive relationship.
5. Calculate the slope of the relationship between 3,846 and 4,071 theatres.

The slope equals the change in revenue per theatre divided by the change in the number of theatres. The slope equals ( $\$ 9,362-\$ 15,867) /(4,071-3,846)$, which equals $-\$ 28.91$ per theatre.
6. Calculate the slope of the relationship between 4,071 and 3,143 theatres.

The slope equals the change in revenue per theatre divided by the change in the number of theatres. The slope equals ( $\$ 6,600-\$ 9,362$ )/(3,143-4,071), which equals $\$ 2.98$ per theatre.
7. Calculate the slope of the relationship shown in Figure A1.1.

The slope is $-5 / 4$. The curve is a straight line, so its slope is the same at all points on the curve. Slope equals the change in the variable measured on the $y$-axis divided by the change in the variable measured on the $x$-axis. To calculate the slope, select two points on the line. One point is at 10 on the $y$-axis and 0 on the $x$-axis, and another is at 8 on the $x$-axis and 0 on the $y$-axis. The change in $y$ from 10 to 0 is associated with the change in $x$ from 0 to 8 . The slope of the curve equals $-10 / 8$, which equals $-5 / 4$.

FIGURE Al. 1
Problem 7


Use the relationship shown in Figure
A1.2 to work Problems 8 and 9.
8. Calculate the slope of the relationship at point $A$ and at point $B$.

The slope at point $A$ is -2 , and the slope at point $B$ is -0.25 . To calculate the slope at a point on a curved line, draw the tangent to the curved line at the point. Then find a second point on the tangent and calculate the slope of the tangent.
The tangent at point $A$ cuts the $y$-axis at 10 . The slope of the tangent equals the change in $y$ divided by the change in $x$. The change in $y$ equals -4 ( 6 minus 10 ) and the change in $x$ equals 2 ( 2 minus 0 ). The slope at point $A$ is $-4 / 2$, which equals -2 .
The tangent at point $B$ goes through the point $(4,2)$. The change in $y$ equals -0.5 , and the change in $x$ equals 2 . The slope at point $B$ is

FIGURE Al. 2
Problems 8 and 9

9. Calculate the slope across the arc $A B$.

The slope across the $\operatorname{arc} A B$ is -1.125 . The slope across the $\operatorname{arc} A B$ equals the change in $y$, which is 4.5 ( 6.0 minus 1.5) divided by the change in $x$, which equals -4 ( 2 minus 6 ). The slope across the arc $A B$ equals $4.5 /-4$, which is -1.125 .

Use the table to work Problems 10 and 11. The table gives the price of a balloon ride, the temperature, and the number of rides a day.
10. Draw a graph to show the relationship between the price and the number of rides, when temperature is $20^{\circ} \mathrm{C}$. Describe this relationship.

The graph plots the price on the $y$ -

| Price <br> (dollars per <br> ride) | Balloon rides <br> (number per day) |  |  |
| :---: | :---: | :---: | :---: |
|  | $10^{\circ} \mathrm{C}$ | $20^{\circ} \mathrm{C}$ | $30^{\circ} \mathrm{C}$ |
| 5 | 32 | 40 | 50 |
| 10 | 27 | 32 | 40 |
| 15 | 18 | 27 | 32 | axis and the number of rides on the $x$-axis using the number of balloon rides in the column of the table labelled $20^{\circ} \mathrm{C}$. The relationship between the price and the number of rides is negative. As the price rises, the number of rides decreases.

11. What happens in the graph in Problem 10 if the temperature rises to $30^{\circ} \mathrm{C}$ ?

If the temperature rises to $30^{\circ} \mathrm{C}$, the curve shifts rightward. At every price, more balloon rides are taken when the temperature is $30^{\circ} \mathrm{C}$ rather than $20^{\circ} \mathrm{C}$.

## Answers to Appendix Additional Problems and Applications

Use the spreadsheet to work Problems 12 to 14. The spreadsheet provides data on oil and gasoline: Column $A$ is the year, column $B$ is the price of oil (dollars per barrel), column C is the price of gasoline (cents per litre), column D is oil production, and column $E$ is the quantity of gasoline refined (both in millions of barrels per day).

|  | A | B | C | D | E |
| :---: | ---: | ---: | :---: | :---: | :---: |
| 1 | 2006 | 66 | 262 | 5.1 | 15.6 |
| 2 | 2007 | 72 | 284 | 5.1 | 15.4 |
| 3 | 2008 | 100 | 330 | 5.0 | 15.3 |
| 4 | 2009 | 62 | 241 | 5.4 | 14.8 |
| 5 | 2010 | 79 | 284 | 5.5 | 15.2 |
| 6 | 2011 | 95 | 358 | 5.6 | 15.1 |
| 7 | 2012 | 94 | 368 | 6.5 | 15.5 |
| 8 | 2013 | 98 | 358 | 7.5 | 15.2 |
| 9 | 2014 | 93 | 344 | 8.8 | 15.5 |
| 10 | 2015 | 49 | 252 | 9.4 | 16.6 |
| 11 | 2016 | 45 | 225 | 9.0 | 16.4 |

12. Draw a scatter diagram of the price of oil and the quantity of oil produced. Describe the relationship.

The scatter diagram between the price of a barrel of oil and the quantity of oil produced shows a weak negative relationship.
13. Draw a scatter diagram of the price of gasoline and the quantity of gasoline refined. Describe the relationship.

The scatter diagram between the price of a gallon of gasoline and the quantity of gasoline refined shows a weak negative relationship.
14. Draw a scatter diagram of the quantity of oil produced and the quantity of gasoline refined. Describe the relationship.
The scatter diagram between the quantity of oil produced and the quantity of gasoline refined shows a positive relationship.

Use the following data to work Problems 15 to 17.

| Draw a | $x$ | 0 | 1 | 2 | 3 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| graph | $y$ | 25 | 24 | 22 | 18 |

FIGURE A1.3
Problems 15, 16, and 17
that
shows the relationship between the two variables $x$ and $y$ in the table below.

To make a graph that shows the relationship between $x$ and $y$, plot the $x$ variable on the $x$-axis and the $y$-variable on the $y$-axis. The graph is shown in Figure A1.3.
15. a. Is the relationship positive or negative?
The relationship is negative because $x$ and $y$ move in opposite directions: As $x$ increases, $y$ decreases.

b. Does the slope of the relationship become steeper or flatter as the value of $\boldsymbol{x}$ increases?

The slope becomes steeper as $x$ increases.
c. Think of some economic relationships that might be similar to this one.

The less expensive a good, the greater is the number of people who buy it. The higher the interest rate, the smaller is the number of people who take out home mortgages. The less expensive gasoline, the greater the miles car owners drive.
16. Calculate the slope of the relationship between $x$ and $y$ when $x$ equals 3 .

The slope equals -5 . The slope of the curve at the point where $x$ is 3 is equal to the slope of the tangent to the curve at that point. Draw the tangent line at the point in Figure A1.3 where $x$ is 3 and $y$ is 18 . Now calculate the slope of this tangent line by finding another point on the tangent. When $x$ equals $5, y$ equals 10 on the tangent, so another point is $x$ equals 5 and $y$ equals 10 . The slope equals the change in $y,-8$, divided by the change in $x, 2$, so the slope is -4.
17. Calculate the slope of the relationship across the arc as $x$ increases from 4 to 5 . The slope is -12 . The slope of the relationship across the arc when $x$ increases from 4 to 5 is equal to the slope of the straight line joining the points on the curve at $x$ equals 4 and $x$ equals 5. When $x$ increases from 4 to $5, y$ falls from 12 to 0 . The slope equals the change in $y,-12$ ( 0 minus 12), divided by the change in $x, 1$ ( 5 minus 4), so the slope across the arc is -12 .
18. Calculate the slope of the curve in Figure A 1.4 at point $A$.

The slope is -2 . The curve is a straight line, so its slope is the same at all points on the curve. Slope equals the change in the variable measured on the $y$-axis divided by the change in the variable measured on the $x$-axis. To calculate the slope, select two points on the line. One point is at 18 on the $y$-axis and 0 on the $x$ axis, and another is at 9 on the $x$-axis and 0 on the $y$-axis. The change in $y$ from 18 to 0 is associated with the change in $x$ from 0 to 9 . Therefore the slope of the curve is $-18 / 9$, which equals -2 .

FIGURE A1.4
Problem 18


Use Figure A1.5 to work Problems 19 and 20.
19. Calculate the slope at point $A$ and at point $B$.

The slope at point $A$ is -4 , and the slope at point $B$ is -1 . To calculate the slope at a point on a curved line, draw the tangent to the line at the point. Then find a second point on the tangent and calculate the slope of the tangent.
The tangent at point $A$ cuts the $x$-axis at 2.5. The slope of the tangent equals the change in $y$ divided by the change in $x$. The change in $y$ equals 6 ( 6 minus 0 ) and the change in $x$ equals -1.5 ( 1 minus 2.5). The slope at point $A$ is $6 /-1.5$, which equals -4 . Similarly, the slope at point $B$ is -1 . The tangent at point $B$ cuts the $y$ axis at 5 . The change in $y$ equals 3 , and the change in $x$ equals -3 .
20. Calculate the slope across the arc $A B$.

## FIGURE A1.5

Problems 19 and 20


The slope across the arc $A B$ is -2 . The slope across the arc $A B$ equals the change in $y$, which is 4 ( 6 minus 2 ) divided by the change in $x$, which equals -2 ( 1 minus 3 ). The slope across the arc $A B$ is $4 /-2$, which equals -2 .
Use the following table to work Problems 21 to 23.
The table gives information about umbrellas: price, the number purchased, and rainfall in millimeters (mms).
21.

|  | Umbrellas |  |  |
| :---: | :---: | :---: | :---: |
| Price |  |  |  |
| (dollars per |  |  |  |
| umbrella) |  |  |  |$\quad$| (number purchased per day) |  |  |  |
| :---: | :---: | :---: | :---: |
|  | 0 mm | 200 mm | 400 mm |
| 20 | 4 | 7 | 8 |
| 30 | 2 | 4 | 7 |
| 40 | 1 | 2 | 4 |

Draw a graph to show relationship between the price and the number of umbrellas purchased, holding the amount of rainfall constant at 200 mm . Describe this relationship.
To draw a graph of the relationship between the price and the number of umbrellas when the rainfall equals 200 mm , keep the rainfall at 200 mm and plot the data in that column against the price. The relationship between the price and the number of umbrellas is a negative relationship.
22. What happens in the graph in Problem 21 if the price rises and rainfall is constant?

If the price rises, the number of umbrellas decreases. There is a movement upward along the (unchanged) curve.
23. What happens in the graph in Problem 21 if the rainfall increases from 200 mm to 400 mm ?

The curve when the rainfall is 400 mm lies to the right of the curve when the rainfall is 200 mm showing that at every price, more umbrellas are purchased when the rainfall is 400 mm than when the rainfall is 200 mm .

